Quantumlike Chaos in the Frequency Distributions of the Bases A, C, G, T in Drosophila DNA

A. M. Selvam

Deputy Director (Retired)
Indian Institute of Tropical Meteorology

Pune 411 008, India

email: amselvam@eth.net

websites: http://amselvam.tripod.com/index.html

http://www.geocities.com/amselvam

Continuous periodogram power spectral analyses of *fractal* fluctuations of frequency distributions of bases A, C, G, T in Drosophila DNA show that the power spectra follow the universal inverse power-law form of the statistical normal distribution. Inverse power-law form for power spectra of space-time fluctuations is generic to dynamical systems in nature and is identified as *self-organized criticality*. The author has developed a general systems theory, which provides universal quantification for observed *self-organized criticality* in terms of the statistical normal distribution. The long-range correlations intrinsic to *self-organized criticality* in macro-scale dynamical systems are a signature of quantumlike chaos. The *fractal* fluctuations self-organize to form an overall logarithmic spiral trajectory with the quasiperiodic *Penrose* tiling pattern for the internal structure. Power spectral analysis

resolves such a spiral trajectory as an eddy continuum with embedded dominant wavebands. The dominant peak periodicities are functions of the *golden mean*. The observed *fractal* frequency distributions of the Drosophila DNA base sequences exhibit quasicrystalline structure with long-range spatial correlations or *self-organized criticality*. Modification of the DNA base sequence structure at any location may have significant noticeable effects on the function of the DNA molecule as a whole. The presence of non-coding *introns* may not be redundant, but serve to organize the effective functioning of the coding *exons* in the DNA molecule as a complete unit.

Keywords: long-range correlations in DNA base sequence, self-organized criticality, quantumlike chaos, quasiperiodic Penrose tiling pattern

1. Introduction

1.1 The DNA molecule and heredity

Heredity in living organisms is determined by a long complex chemical molecule called DNA (deoxyribonucleic acid). The units of heredity, the genes are parts of the DNA molecule situated along the length of the chromosomes inside the nucleus of the cell. A simplified picture of the molecule of DNA may be visualised to consist of two long backbones with projections sticking out from them at right angles rather like a ladder with its two upright sides and its rungs. The backbones are made up of two simple chemicals arranged alternately - *sugar* - *phosphate* - *sugar* - *phosphate* - all along the way. The projections are the four units or 'letters' of the code; they are four chemical bases called *guanine*, *cytosine*, *adenine* and *thymine* - G, C, A, T. These four bases are arranged in a specific sequence, which constitutes the genetic code. The DNA molecule actually consists not

of a single thread, but of two helical threads wound around each other - a double helix. The two DNA chains run in opposite directions and are coiled around each other with the bases facing one another in pairs. Only specific pairs of bases can be linked together, T always pairs with A, and G with C (Claire, 1964; Bates and Maxwell, 1993). The amount of A is the same as the amount of T, while the amount of G is the same as the amount of C. These are now known as Chargaff ratios (Gribbin, 1985; Alcamo, 2001).

What distinguishes one type of cell from another and one organism from another is the protein, which it contains. And it is DNA which dictates to the cell how many and what types of protein it shall make. Twenty different chemicals called amino acids in different sets of combinations form the proteins. The sequence of bases along each DNA molecule in the chromosome determines the sequence of amino acids along each of the proteins. It takes a sequence of 3 bases, the codon, to identify one amino acid. The order in which these bases recur within a particular gene in the helix corresponds to the information needed to build that gene's particular protein (Claire, 1964; Leone, 1992; Ball, 2000).

The genes of higher organisms are seldom 'recorded' in the chromosomes intact, but are scattered in fragmentary fashion along a stretch of DNA, broken up by chunks of DNA which seem at first sight to carry no message at all. All the useless or "junk" DNA, the intervening sequences are known as *introns*. The pieces of DNA carrying genetic code are called *exons*. The codons, *64* in number are distributed over the coding parts of the DNA sequences. It is well known that the coding regions are translated into proteins. The noncoding parts are presumed important in regulatory and promotional activities. The biologically meaningful structures in non-coding regions are not known (Gribbin, 1985; Guharay et al. 2000; Clark,

2001; Som et al., 2001). Understanding genetic defects will make it easier to treat them (Watson, 1997).

Historically, Watson and Crick (1953) put together all the experimental data concerning DNA and decided that the only structure that fitted all the facts was the double helix and postulated that DNA is composed of two ribbonlike "backbones" composed of alternating deoxyribose and phosphate molecules. They surmised that nucleotides extend out from the backbone chains and that the 0.34nm distance represents the space between successive nucleotides. The Xray data showed a distance of 34nm between turns, so they guessed that ten nucleotides exist per turn. One strand of DNA would only encompass Inm width, so they postulated that DNA is composed of two strands to conform to the 2nm diameter observed in the X-ray diffraction photographs. Scientists now agree that DNA is arranged as a double helix of two intertwined chains, with complementary bases (A-T and G-C) opposing each other. Moreover, the strands run opposite to one another, that is, the strands display the reverse polarity. Given the base sequence of one chain of DNA, the base sequence of its partner chain is automatically determined by simply noting which bases are complimentary (adenine-thymine or cytosineguanine). Furthermore, the structure provides a mechanism by which one chain can serve as a template (a model or pattern) for the synthesis of the other chain (Sambamurty, 1999; Alcamo, 2001). The genomic DNA in cells must be highly compacted in order to be contained in the required space. Each chromosome appears to contain a single giant molecule of DNA. At least three levels of condensation are required to package the 10^3 to 10^5 micrometer of DNA in a eukaryotic (higher organism) chromosome into a metaphase structure a few microns long. The first level of condensation involves packaging DNA as a supercoil into nucleosomes. This produces 10nm diameter interphase chromatin fibre. Second level of condensation involves an additional folding and/or supercoiling of the 10nm nucleosome fibre to produce the 30nm chromatin fibre. This third level of condensation appears to involve the segregation of segments of the giant DNA molecules present in eukaryotic chromosomes into independently supercoiled domains or loops. The mechanism by which this third level of condensation occurs is not known (Sambamurty, 1999).

1.2 Long-range correlations in DNA base sequence

DNA topology is of fundamental importance for a wide range of biological processes (Bates and Maxwell, 1993). One big question in DNA research is whether there is some meaning to the order of the base pairs in DNA. Human DNA has become a fascinating topic for physicists to study. One reason for this fascination is the fact that when living cells divide, the DNA is replicated exactly. This is interesting because approximately 95% of human DNA is called "junk" even by biologists who specialize in DNA. One practical task for physicists is simply to identify which sequences within the molecule are the coding sequences. Another scientific interest is to discover why the "junk" DNA is there in the first place. Almost everything in biology has a purpose that, in principle, is discoverable (Stanley, 2000). The study of statistical patterns in DNA sequences is important as it may improve our understanding of the organization and evolution of life on the genomic level. Recent studies indicate that the DNA sequence of letters A, C, G and T does have a $1/f^a$ frequency spectrum where f is the frequency and a the exponent. It is possible, therefore, that the sequences have long-range order and underlying grammar rules. The opinion on this issue remains divided (Som et al., 2001 and all references therein). The findings of longrange correlations in DNA sequences have attracted much attention, and attempts have been made to relate those findings to known

biological features such as the presence of triplet periodicities in protein-coding DNA sequences, the evolution of DNA sequences, the length distribution of protein-coding regions, or the expansion of simple sequence repeats (Holste *et al.*, 2001).

A summary of recent results relating to long-range correlation (LRC) in DNA sequences is given in the following. Based on spectral analyses, Li et al. found (Li, 1992; Li and Kaneko, 1992; Li, Marr and Kaneko, 1994) that the frequency spectrum of a DNA sequence containing mostly introns shows 1/f^{\alpha} behavior, which evidences the presence of long-range correlations. The correlation properties of coding and non-coding DNA sequences were first studied by Peng et al. (1992) in their fractal landscape or DNA walk model. Peng et al. (1992) discovered that there exists LRC in non-coding DNA sequences while the coding sequences correspond to a regular random walk. By doing a more detailed analysis of the same data set, Chatzidimitriou-Dreismann and Larhammar (1993) concluded that both coding and non-coding sequences exhibit LRC. A subsequent work by Prabhu and Claverie (1992) also substantially corroborates these results. Buldyrev et al. (1995) showed the LRC appears mainly in non-coding DNA using all the DNA sequences available. Alternatively, Voss (1992; 1994), based on equal-symbol correlation, showed a power-law behavior for the sequences studied regardless of the percent of intron contents. Havlin et al. (1995) state that DNA sequence in genes containing non-coding regions is correlated, and that the correlation is remarkably long range--indeed, base pairs thousands of base pairs distant are correlated. Such long-range correlations are not found in the coding regions of the gene. Havlin et al. (1995) suggest that non-coding regions in plants and invertebrates may display a smaller entropy and larger redundancy than coding regions, further supporting the possibility that non-coding regions of DNA may carry biological information. Investigations based on

different models seem to suggest different results, as they all look into only a certain aspect of the entire DNA sequence. It is therefore important to investigate the degree of correlations in a modelindependent way. Hence one may ignore the composition of the four kinds of bases in coding and non-coding segments and only consider the rough structure of the complete genome or long DNA sequences. Yu et al. (2000) proposed a time series model based on the global structure of the complete genome and considered three kinds of length sequences. The values of the exponents from these three kinds of length sequences of bacteria indicate that the long-range correlations exist in most of these sequences (Yu et al., 2000 and all the references contained therein). Recently from a systematic analysis of human exons, coding sequences (CDS) and introns, Audit et al. (2001) have found that power law correlations (PLC) are not only present in non-coding sequences but also in coding regions somehow hidden in their inner codon structure. If it is now well admitted that long-range correlations do exist in genomic sequence, their biological interpretation is still a continuing debate (Audit et al., 2001 and all references therein).

The long-range correlation does not necessarily imply a deviation from Gaussianity. For example, the fractional Brownian motion, which has Gaussian statistics, shows an inverse power-law spectrum. According to Allegrini *et al.* (1996, based on Levy's statistics), long-range correlations would imply a strong deviation from Gaussian statistics while the investigation of Arneodo *et al.* (1995) yields an important conclusion that the DNA statistics are essentially Gaussian (Mohanty and Narayana Rao, 2000).

In visualizing very long DNA sequences, including the complete genomes of several bacteria, yeast and segments of human genes, it is seen that *fractal*-like patterns underlie these biological objects of prominent importance. The method used to visualize genomes of

organisms may well be used as a convenient tool to trace, e.g., evolutionary relatedness of species (Hao *et al.*, 2000). Stanley, Amaral *et al.* (1996) and Stanley, Afanasyev *et al.* (1996) discuss examples of complex systems composed of many interacting subsystems, which display nontrivial long-range correlations or long-term "memory". The statistical properties of DNA sequences, heartbeat intervals, brain plaque in Alzheimer brains, and fluctuations in economics have the common feature that the guiding principle of scale invariance and universality appear to be relevant (Stanley, 2000).

1.3 Nonlinear dynamics and chaos

Irregular (nonlinear) fluctuations on all scales of space and time are generic to dynamical systems in nature such as fluid flows, atmospheric weather patterns, heart beat patterns, stock market fluctuations, etc. Mandelbrot (1977) coined the mme fractal for the non-Euclidean geometry of such fluctuations which have fractional dimension, for example, the rise and susequent fall with time of the Dow Jones Index or rainfall traces a zig-zag line in a two-dimensional plane and therefore has a fractal dimension greater than one but less than two. Mathematical models of dynamical systems are nonlinear finite precision computer realizations exhibit dependence on initial conditions resulting in chaotic solutions, identified as deterministic chaos. Nonlinear dynamics and chaos is now (since 1980s) an area of intensive research in all branches of science (Gleick, 1987). The fractal fluctuations exhibit scale invariance or selfsimilarity manifested as the widely documented (Bak, Tang, Wiesenfeld, 1988; Bak and Chen, 1989; 1991; Schroeder, 1991; Stanley, 1995; Buchanan, 1997) inverse power-law form for power spectra of space-time fluctuations identified as selforganized criticality by Bak et al. (1987). The power-law is a distinctive experimental signature seen in a wide variety of complex systems. In economy it goes by the name fat tails, in physics it is referred to as critical fluctuations, in computer science and biology it is the edge of chaos, and in demographics it is called Zipf's law (Newman, 2000). Power-law scaling is not new to economics. The power-law distribution of wealth discovered by Vilfredo Pareto (1848-1923) in the 19th century (Eatwell, Milgate and Newman, 1991) predates any power-laws in physics (Farmer, 1999). One of the oldest scaling laws in geophysics is the *Omori law* (Omori, 1895). It describes the temporal distribution of the number of aftershocks, which occur after a larger earthquake (i.e., mainshock) by a scaling relationship. The other basic empirical seismological law, the Gutenberg-Richter law (Gutenberg and Richter, 1944) is also a scaling relationship, and relates intensity to its probability of occurrence (Hooge et. al., 1994). Time series analyses of global market economy also exhibits power-law behaviour (Bak et al., 1992; Mantegna and Stanley, 1995; Sornette et al., 1995; Chen, 1996a,b; Stanley, Amaral, Buldyrev, Havlin et al., 1996; Feigenbaum and Freund, 1997a,b; Gopikrishnan et al., 1999; Plerou et al., 1999; Stanley et al., 2000; Feigenbaum, 2001a, b) with possible multifractal structure (Farmer, 1999) and has suggested an analogy to fluid turbulence (Ghashghaie et al., 1996; Arneodo et al., 1998). Sornette et al. (1995) conclude that the observed power law represents structures similar to Elliott waves of technical analysis first introduced in the 1930s. It describes the time series of a stock price as made of different waves; these waves are in relation to each other through the Fibonacci series. Sornette et al. (1995) speculate that Elliott waves could be a signature of an underlying critical structure of the stock market. Incidentally the Fibonacci series represent a fractal tree-like branching network of selfsimilar structures (Stewart, 1992). The commonly found shapes in nature are the helix and the dodecahedron

(Muller and Beugholt, 1996), which are signatures of selfsimilarity underlying *Fibonacci* numbers. The general systems theory presented in this paper shows (Section 2) that *Fibonacci* series underlies *fractal* fluctuations on all space-time scales.

Historically, basic similarity in the branching (fractal) form underlying the individual leaf and the tree as a whole was identified more than three centuries ago in botany (Arber, 1950). The branching (bifurcating) structure of roots, shoots, veins on leaves of plants, etc., have similarity in form to branched lighting strokes, tributaries of rivers, physiological networks of blood vessels, nerves and ducts in lungs, heart, liver, kidney, brain, etc. (Freeman, 1987; 1990; Goldberger et al., 1990; Jean, 1994;). Such seemingly complex network structure is again associated with Fibonacci numbers seen in the exquisitely ordered beautiful patterns in flowers and arrangement of leaves in the plant kingdom (Jean, 1994; Stewart, 1995). The identification of physical mechanism for the spontaneous generation of mathematically precise, robust spatial pattern formation in plants will have direct applications in all other areas of science (Mary Selvam, 1998). The importance of scaling concepts were recognized nearly a century ago in biology and botany where the dependence of a property y on size x is usually expressed by the allometric equation $y=ax^{b}$ where a and b are constants (Thompson, 1963; Strathmann, 1990; Jean, 1994; Stanley, Amaral, Buldyrev, Goldberger et al., 1996). This type of scaling implies a hierarchy of substructures and was used by D'Arcy Thompson for scaling anatomical structures, for example, how proportions tend to vary as an animal grows in size (West, 1990a). D'Arcy Thompson (1963, first published in 1917) in his book On Growth and Form has dealt extensively with similitude principle for biological modelling. Rapid advances have been made in recent years in the fields of biology and medicine in the application of scaling (fractal) concepts for description and quantification of physiological systems and their functions (Goldberger, Rigney and West, 1990; West, 1990a,b; Deering and West, 1992; Skinner, 1994; Stanley, Amaral, Buldyrev, Goldberger *et. al.*, 1996). In meteorological theory, the concept of selfsimilar fluctuations was identified and introduced in the description of turbulent flows by Richardson (1965, originally published in 1922; see also Richardson, 1960), Kolmogorov (1941, 1962), Mandelbrot (1975) (Kadanoff 1996) and others (see Monin and Yaglom, 1975 for a review).

Self-organized criticality implies long-range space-time correlations or non-local connections in the spatially extended dynamical system. The physics underlying self-organized criticality is not yet identified. Prediction of the future evolution of the dynamical system requires precise quantification of the observed self-organized criticality. The author has developed a general systems theory (Capra, 1996), which predicts the observed self-organized criticality as a signature of quantumlike chaos in the macro-scale dynamical system (Mary Selvam, 1990; Mary Selvam, Pethkar and Kulkarni, 1992; Selvam and Fadnavis, 1998). The model also provides universal and unique quantification for the observed self-organized criticality in terms of the statistical normal distribution.

Continuous periodogram power spectral analyses of the frequency distribution of bases A, C, G, T in Drosophila DNA base sequence agree with model prediction, namely, the power spectra follow the universal inverse power law form of the statistical normal distribution. The geometrical distribution in space, of the DNA bases, therefore exhibit *self-organized criticality*, which is a signature of quantumlike chaos. Earlier studies by the author have identified quantumlike chaos exhibited by dynamical systems underlying the observed *fractal* fluctuations of the following data sets: (1) Time series of meteorological parameters (Mary Selvam, Pethkar and Kulkarni, 1992; Selvam and Joshi, 1995; Selvam *et al.*, 1996; Selvam

and Fadnavis, 1998). (2) Spacing intervals of adjacent prime numbers (Selvam and Suvarna Fadnavis, 1998; Selvam, 2001a) (3) Spacing intervals of adjacent non-trivial zeros of the Riemann zeta function (Selvam, 2001b).

2. General Systems Theory for Universal Quantification of Fractal Fluctuations of Dynamical Systems

As mentioned earlier (Section 1.3) power spectral analyses of *fractal* space-time fluctuations of dynamical systems exhibits inverse power-law form, i.e., a selfsimilar eddy continuum. The cell dynamical system model (Mary Selvam, 1990; Selvam and Fadnavis, 1998, and all references contained therein; Selvam, 2001a, b) is a general systems theory (Capra, 1996) applicable to dynamical systems of all size scales. The model shows that such an eddy continuum can be visualised as a hierarchy of successively larger scale eddies enclosing smaller scale eddies. Eddy or wave is characterised by circulation speed and radius. Large eddies of root mean square (r.m.s) circulation speed W and radius R form as envelopes enclosing small eddies of r.m.s circulation speed W and radius R form as envelopes enclosing small eddies of r.m.s circulation speed W and radius R form as envelopes enclosing small eddies of

$$W^2 = \frac{2}{\mathbf{p}} \frac{r}{R} w_*^2 \tag{1}$$

Since the large eddy is but the average of the enclosed smaller eddies, the eddy energy spectrum follows the statistical normal distribution according to the *Central Limit Theorem* (Ruhla, 1992). Therefore, the variance represents the probability densities. Such a result that the additive amplitudes of eddies, when squared, represent the probabilities is an observed feature of the subatomic dynamics of quantum systems such as the electron or photon (Maddox 1988a,

1993; Rae, 1988). The *fractal* space-time fluctuations exhibited by dynamical systems are signatures of quantumlike mechanics. The cell dynamical system model provides a unique quantification for the apparently chaotic or unpredictable nature of such *fractal* fluctuations (Selvam and Fadnavis, 1998). The model predictions for quantumlike chaos of dynamical systems are as follows.

- The observed *fractal* fluctuations of dynamical systems are generated by an overall logarithmic spiral trajectory with the quasiperiodic *Penrose* tiling pattern (Nelson, 1986; Selvam and Fadnavis, 1998) for the internal structure.
- Conventional continuous periodogram power spectral analyses of such spiral trajectories will reveal a continuum of periodicities with progressive increase in phase.
- The broadband power spectrum will have embedded dominant wavebands, the bandwidth increasing with period length. The peak periods (or length scales) E_n in the dominant wavebands is given in terms of t, the golden mean equal to $(1+\ddot{0}\ 5)/2$ [@ 1.618] and T_s , the primary perturbation length scale as

$$E_n = T_S(2+t)t^n \tag{2}$$

Considering the most representative example of turbulent fluid flows, namely, atmospheric flows, Ghil (1994) reports that the most striking feature in climate variability on all time scales is the presence of sharp peaks superimposed on a continuous background. The model predicted periodicities (or length scales) in terms of the primary perturbation length scale units are 2.2, 3.6, 5.8, 9.5, 15.3, 24.8, 40.1, 64.9, 105.0 respectively for values of n ranging from -1 to 7. Periodicities (or length scales) close to model predicted have been reported in weather and climate variability (Burroughs, 1992; Kane, 1996), prime

number distribution (Selvam, 2001a), Riemann zeta zeros (nontrivial) distribution (Selvam, 2001b).

As mentioned earlier Sornette *et al.* (1995) also conclude that the observed power-law represents structures similar to *Elliott waves* of technical analysis first introduced in the 1930s. It describes the time series of a stock price as made of different waves; these waves are in relation to each other through the *Fibonacci* series.

- The length scale ratio r/R also represents the increment dq in phase angle q (Equation 1). Therefore the phase angle q represents the variance. Hence, when the logarithmic spiral is resolved as an eddy continuum in conventional spectral analysis, the increment in wavelength is concomitant with increase in phase (Selvam and Fadnavis, 1998). Such a result that increments in wavelength and phase angle are related is observed in quantum systems and has been named Berry's phase (Berry 1988; Maddox 1988b; Simon et al., 1988; Anandan, 1992). The relationship of angular turning of the spiral to intensity of fluctuations is seen in the tight coiling of the hurricane spiral cloud systems.
- The overall logarithmic spiral flow structure is given by the relation

$$W = \frac{W_*}{k} \log z \tag{3}$$

• The constant k in Equation 3 is the steady state fractional volume dilution of large eddy by inherent turbulent eddy fluctuations. The constant k is equal to $1/\mathbf{t}^2 \cong 0.382$ and is identified as the universal

constant for deterministic chaos in fluid flows (Selvam and Fadnavis, 1998). The steady state emergence of *fractal* structures is therefore equal to

$$\frac{1}{k} \cong 2.62 \tag{4}$$

The model predicted logarithmic wind profile relationship such as Equation 3 is a long-established (observational) feature of atmospheric flows in the atmospheric boundary layer, the constant k, called the *Von Karman*'s constant has the value equal to 0.38 as determined from observations (Wallace and Hobbs, 1977).

In Equation 3, W represents the standard deviation of eddy fluctuations, since W is computed as the r.m.s. (root mean square) eddy instantaneous perturbation amplitude with reference to the earlier step of eddy growth. For two successive stages of eddy growth starting from primary perturbation w_* the ratio of the standard deviations W_{n+1} and W_n is given from Equation 3 as (n+1)/n. Denoting by s the standard deviation of eddy fluctuations at the reference level (n=1), the standard deviations of eddy fluctuations for successive stages of eddy growth are given as integer multiple of s, i.e., s, 2s, 3s, etc., and correspond respectively to statistical normalized standard deviation t=0, 1, 2, 3, etc.

statistical normalized standard deviation $t = 0, 1, 2, 3, \dots$ (5)

 The conventional power spectrum plotted as the variance versus the frequency in log-log scale will now represent the eddy probability density on logarithmic scale versus the standard deviation of the eddy fluctuations on linear scale since the logarithm of the eddy wavelength represents the standard deviation, i.e., the r.m.s. value of eddy fluctuations (Equation 3). The r.m.s. value of eddy fluctuations can be represented in terms of statistical normal distribution as follows. A normalized standard deviation t=0 corresponds to cumulative percentage probability density equal to 50 for the mean value of the distribution. Since the logarithm of the wavelength represents the r.m.s. value of eddy fluctuations the normalized standard deviation t is defined for the eddy energy as

$$t = \frac{\log L}{\log T_{50}} - 1 \tag{6}$$

The parameter L in Equation 6 is the wavelength (or period) and T_{50} is the wavelength (or period) up to which the cumulative percentage contribution to total variance is equal to 50 and t = 0. The variable $log T_{50}$ also represents the mean value for the r.m.s. eddy fluctuations and is consistent with the concept of the mean level represented by r.m.s. eddy fluctuations. Spectra of time series of fluctuations of dynamical systems, for example, meteorological parameters, when plotted as cumulative percentage contribution to total variance versus t follow the model predicted universal spectrum (Selvam and Fadnavis, 1998, and all references therein). The literature shows examples of pressure, wind and temperature whose shapes display a remarkable degree of universality (Canavero and Einaudi, 1987).

The periodicities (or length scales) T_{50} and T_{95} up to which the cumulative percentage contribution to total variances are respectively equal to 50 and 95 are computed from model concepts as follows. The power spectrum, when plotted as normalised standard deviation t versus cumulative percentage contribution to represents the statistical total variance distribution (Equation 6), i.e. the variance represents the probability density. The normalised standard deviation values t corresponding to cumulative percentage probability densities P equal to 50 and 95 respectively are equal to θ and 2 from statistical normal distribution characteristics. Since t represents the eddy growth step n (Equation 5) the dominant periodicities (or length scales) T_{50} and T_{95} up to which the cumulative percentage contribution to total variance respectively equal to 50 and 95 are obtained from Equation 2 for corresponding values of n equal to θ and 2. In the present study of fractal fluctuations of frequency distribution of Drosophila DNA bases A, C, G, T, the primary perturbation length scale T_s is equal to unit length segment of 50 bases and T_{50} and T_{95} are obtained as

$$T_{50} = (2 + \mathbf{t})\mathbf{t}^0 \cong 3.6 \text{ unit length segment of } 50 \text{ bases}$$
 (7)

$$T_{95} = (2 + t)t^2 \cong 9.5$$
 unit length segment of 50 bases (8)

The above model predictions are applicable to all real world and computed model dynamical systems. Continuous periodogram power spectral analyses of number frequency (per 50 bases) of occurrence of bases A, C, G, T in Drosophila DNA base sequence

at different locations along its length give results in agreement with the above model predictions.

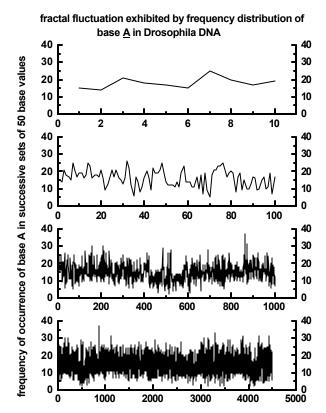
3. Data and Analysis

The Drosophila DNA base sequence was obtained from Berkeley Project (BGDP Drosophila Genome Resources http://www.fruitfly.org/index.html. The data set used for the study corresponds to the file NA ARMS~1 with the title: >2L, 28-11-2001.1 (22207800 bases) segment 1 of 1 for arm 2L on wed Nov 28 00.30.01 **PST** 2001 (http://www.fruitfly.org/sequence/sequence_db/na_arms.dros._RELEASE_2.9) finished sequence for 2L. The first 225000 bases were used to give 50 data sets each of length 4500 bases. The number of times that each of the bases A, C, G, T occur in successive blocks of 50 bases was determined for each data set of 4500 bases. Each data set of 4500 bases then gives 4 groups of 90 frequency sequence values corresponding respectively to the four bases A, C, G, T.

3.1 Fractal nature of frequency distribution of Drosophila DNA base (A, C, G, or T) sequence

A representative sample for the frequency of occurrence of base A in successive blocks of length 50 bases is plotted in Figure 1 for 10, 100, 1000 and 4500 segments for the total sequence consisting of 225000 bases used in the study.

The frequency distribution shows irregular or *fractal* fluctuations for all the segment length scales. The irregular fluctuations may be visualized to result from the superimposition of an ensemble of eddies (wavelengths).



set sequence number: each set consists of 50 base values the first 4500 sets (225000 base values) were used for the study

Figure 1: Fractal nature of frequency distribution of Drosophila DNA base (A, C, G, or T) sequence

3.1 The frequency distributions of DNA bases A, C, G, T and the statistical normal distribution

The frequency distribution of bases A, C, G, T follow statistical normal distribution (Selvam and Suvarna Fadnavis, 2001) as

© 2002 C. Roy Keys Inc.

described in the following. Each data set consists of the frequency distribution X_j where j = 1, 2, ...n denotes the class interval number, the total number n equals 90 class intervals and each class interval consists of 50 bases, so that each data set consists of 4500 bases. The mean Xbar, standard deviation s, and normalised standard deviation t_j for each set of frequency distributions was calculated as follows:

$$mean \ Xbar = \frac{\sum_{j=1}^{n} X_{j} * j}{n}$$

$$standard \ deviation \ s = \sqrt{\frac{\sum_{j=1}^{n} (mean - X_{j})^{2} * j}{n}}$$

The cumulative frequency of occurrence p_j of base (A, C, G or T) for class intervals j = 1, 2, ...n were calculated as

$$p_j = \sum_{i=1}^{j} X_j$$

The cumulative percentage frequency of occurrence p_c of base (A, C, G or T) for class intervals j = 1, 2, ...n were then calculated as

$$p_c = \frac{p_j}{p_n} * 100$$

The graph of cumulative percentage frequency of occurrence p_c versus the corresponding normalised standard deviation t_j follows closely the statistical normal distribution as shown in Figure 2 for all the four bases A, C, G, T in the Drosophila DNA sequence. The above result is consistent with model prediction that the variance spectrum of *fractal* fluctuations follows statistical normal distribution as explained in the following. From Equation (1), namely

 $W^2 = \frac{2}{p} \frac{r}{R} w_*^2$ it is seen that the length scale ratio r/R (or frequency ratio) represents the variance spectrum (W^2/w_*^2) and therefore the cumulative frequency distribution follows closely the cumulative normal distribution as shown in Figure 2.

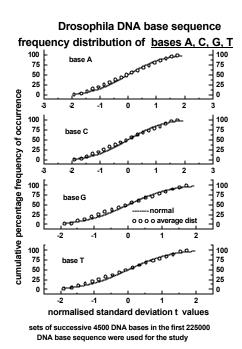
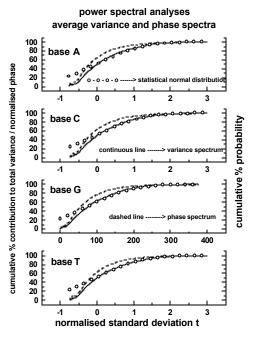


Figure 2: The cumulative percentage frequency of occurrence of bases A, C, G, T in Drosophila DNA sequence follow closely the statistical normal distribution

3.2 Continuous periodogram power spectral analyses

The broadband power spectrum of space-time fluctuations dynamical ofsystems can be computed accurately by an elementary, but very powerful method of analysis developed Jenkinson (1977)which provides a quasi-continuous of the form classical periodogram allowing systematic allocation of the total variance and degrees of freedom of the data series to logarithmically spaced elements of the frequency range (0.5, 0). The periodogram is constructed for a fixed set of 10000(m)wavelengths (or periodicities)



data: frequency distribution of Drosophila DNA bases A, C, G, T

in the present study of Drosophila DNA base sequence structure. The cumulative percentage contribution to total variance was computed starting from the high frequency side of the spectrum. The wavelength (or period) T_{50} at which

 L_m which increase geometrically as $L_m=2$ exp(Cm) where C=.001 and m=0, 1, 2,....m. The data series X_j for the n data points was used. The periodogram estimates the set

$$A_m \cos(2\mathbf{p}\mathbf{n}_m S - \mathbf{f}_m)$$

where A_m , \mathbf{n}_m and \mathbf{f}_m denote respectively the amplitude, frequency and phase angle for the m^{th} wavelength (or periodicity) and S is the spatial (or time) interval in units of 50 bases

Figure 3: Average variance (continuous line) and phase (dashed line) spectra for the bases A, C, G, T for the 50 data sets used in the study. The statistical normal distribution (open circles) is also shown.

wavelength (or period) T_{50} at which 50% contribution to total variance occurs is taken as reference and the normalized standard deviation t_m values are computed as (Equation 6)

$$t_m = \frac{\log L_m}{\log T_{50}} - 1$$

The cumulative percentage contribution to total variance, the cumulative percentage normalized phase (normalized with respect to the total phase rotation) and the corresponding t_m values were computed. The power spectra were plotted as cumulative percentage contribution to total variance versus the normalized standard deviation t_m as given above. The wavelength (or period) L_m is in units of 50 bases as explained above. Wavelengths (or periodicities) up to T_{50} contribute up to 50% of total variance. The phase spectra were plotted as cumulative percentage normalized (normalized to total rotation) phase.

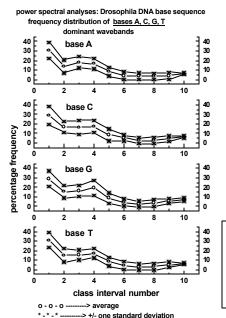
3.4 Power spectral analyses: summary of results

3.4.1 Average variance and phase spectra

The average variance and phase spectra for the 50 data sets used in the study along with statistical normal distribution are shown in Figure 3 for the four bases A, C, G, T. The 'goodness of fit' (statistical chi-square test) between the variance spectra and statistical normal distribution is significant at less than or equal to 5% level for all the variance spectra. The eddy variance spectra following statistical normal distribution is a signature of quantumlike chaos (see Section 2) in the frequency distribution sequence of bases A, C, G, T in Drosophila DNA base sequence arrangement. Phase spectra are close to the statistical normal distribution, with the 'goodness of fit' being statistically significant for 42, 36, 48 and 42 percent of data sets respectively for the four bases A, C, G, T. However, in all the cases, the 'goodness of fit' between variance and phase spectra are statistically significant (chi-square test) for individual dominant wavebands, in particular for shorter wavelengths as shown in Figure 6. Eddy variance spectra following phase spectra is identified as Berry's phase and is also a signature of quantumlike chaos (see Section 1, Equation 1). The data sets, which do not exhibit *Berry's phase*, are indicated in Figure 9.

3.4.2 Dominant wavebands

The power spectra exhibit dominant wavebands where the normalised variance is equal to or greater than I. The dominant peak wavelengths (periodicities) were grouped into class intervals 2 - 3, 3 - 4, 4 - 6, 6 - 12, 12 - 20, 20 - 30, 30 - 50, 50 - 80, 80 - 120. These class intervals include the model predicted (Equation 2) dominant peak periodicities (or length scales) 2.2, 3.6, 5.8, 9.5, 15.3, 24.8, 40.1, 64.9, 105.0, (in block length segment unit of 50 bases) for values of n ranging from -1 to 7. Wavelength class interval-wise percentage frequency of occurrence of dominant periodicities were computed. In each class interval, the number of dominant statistically significant (less than or equal to 5%) periodicities and also the number of dominant



wavebands which exhibit Berry's phase (variance phase spectra are the same) are computed as percentages of the total number of dominant each wavebands in class interval The class interval-wise mean and standard deviation of the above computed frequency distribution dominant ofsignificant periodicities, periodicities dominant and

Figure 4: Average wavelength class interval-wise distribution of dominant wavebands for the four bases A, C, G, T in the 50 data sets (a total of 225000 bases) of Drosophila DNA

dominant periodicities exhibiting *Berry's phase* (see Section 2) were then computed for the four bases A, C, G, T in the Drosophila DNA sequence. The average class interval-wise distribution of dominant wavelengths (periodicities), significant dominant wavelengths and dominant wavelengths exhibiting *Berry's phase* respectively are shown in Figures 4, 5 and 6.

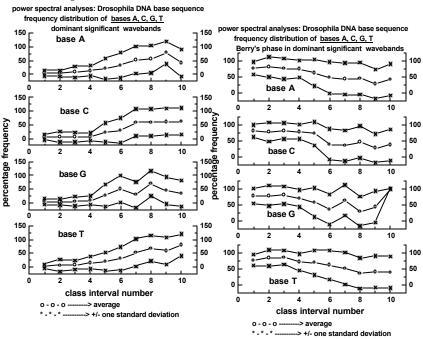


Figure 5: Average wavelength class interval-wise distribution of dominant significant wavebands for the four bases A, C, G, T in the 50 data sets (a total of 225000 bases) of Drosophila DNA base sequence used for the study

Figure 6: Average wavelength class interval-wise distribution of dominant wavebands exhibiting Berry's phase for the four bases A, C, G, T in the 50 data sets (a total of 225000 bases) of Drosophila DNA base sequence used for the study

3.4.3 Peak wavelength versus bandwidth

The model predicts that the apparently irregular *fractal* fluctuations contribute to the ordered growth of the quasiperiodic *Penrose* tiling pattern with an overall logarithmic spiral trajectory such that the successive radii lengths follow the *Fibonacci* mathematical series.

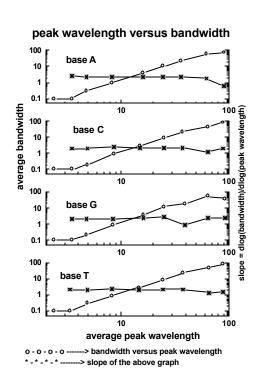


Figure 7: Log-log plot of average values of bandwidth versus peak wavelength for the four bases A, C, G, T. The slope (bandwidth/peak wavelength) of this graph, also plotted in the above figure shows an approximately constant value equal to ~2.

Conventional power spectral analyses resolves such a spiral trajectory as an eddy continuum with embedded dominant wavebands, the bandwidth increasing with wavelength. The progressive increase in the radius of the spiral the trajectory generates bandwidth eddy proportional the to increment d**q** in phase angle equal to r/R. The relative eddy circulation speed W/w* is directly proportional to the relative peak wavelength ratio R/rsince the eddy circulation

speed W=2pR/T where T is the eddy time period. The relationship between the peak wavelength and the bandwidth is obtained

from Equation (1), namely,
$$W^2 = \frac{2}{n} \frac{r}{R} w_*^2$$
.

Considering eddy growth with overall logarithmic spiral trajectory

relative eddy bandwidth
$$\propto d\mathbf{q} \propto \frac{r}{R}$$

The eddy circulation speed is related to eddy radius as

$$W = \frac{2\mathbf{p} R}{T}$$

$$W \propto R \propto peak \text{ wavelength}$$

The relative peak wavelength is given in terms of eddy circulation speed as

relative peak wavelength
$$\propto \frac{W}{w_*}$$

From Equation (1) the relationship between eddy bandwidth and peak wavelength is obtained as

eddy bandwidth =
$$(peak wavelength)^2$$

$$\frac{log(eddy bandwidth)}{log((peak wavelength))} = 2$$
(9)

A log-log plot of peak wavelength versus bandwidth will be a straight line with a slope (bandwidth/peak wavelength) equal to 2. A log-log plot of the average values of bandwidth versus peak wavelength shown in Figure 7 exhibits a constant slope approximately equal to 2 in agreement with the above model prediction.

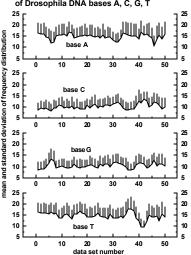
The mean and standard deviation of the frequency distribution for bases A, C, G, T for all the 50 data sets are given in Figure 8. Each data set consists of a sequence of 90 frequency values corresponding

to 90 successive block lengths of 50 bases of Drosophila DNA base sequence.

The periodicities T_{50} up to which the cumulative percentage contribution to total variance is equal to 50 are shown for the bases A, C, G, T for the 50 data sets in Figure 9. The letter 'N' denotes data set

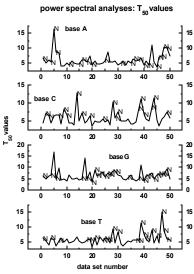
which does not exhibit *Berry's phase*, i.e., the 'goodness of fit' between variance and phase spectra is not significant.

mean and standard deviation of frequency distribution of Drosophila DNA bases A, C, G, T



each data set consists of 90 frequency values corresponding to occurrence of base in successive sets of 50 base values for a total length of 4500 base values for each set

Figure 8: The mean and standard deviation of the frequency distribution for bases A, C, G, T for all the 50 data sets. The vertical line correspond to one standard deviation for the data set.



N indicates phase spectrum does not follow normal distribution variance spectra follow normal distribution for all data sets

Figure 9: The periodicities T₅₀ up to which the cumulative percentage contribution to total variance is equal to 50. The letter 'N' denotes data set which does not exhibit 'Berry's phase', i.e., the 'goodness of fit' between variance and phase spectra is not significant. Variance spectra follow normal distribution for all data sets.

4. Results and Discussion

The number frequency of occurrence of each of the bases A, C, G, T in successive block lengths of 50 bases of Drosophila DNA base sequence exhibit selfsimilar fractal fluctuations generic to dynamical systems in nature. The apparently irregular (chaotic) fractal fluctuations, which characterise the fine-scale geometry of spatial structures in nature, are now an intensive field of study in the new science of Nonlinear Dynamics and Chaos. The fractal fluctuations are basically a zigzag pattern of successive upward and downward swings such as that shown in Figure 1 for the frequency distribution of bases A, C, G, T for all data lengths, i.e., number of blocks ranging from 10 to the maximum 4500, a total of 225000 Drosophila DNA base sequence. Such irregular fluctuations may be visualised to result from the superimposition of a continuum of eddies. Power spectral analysis is commonly applied to resolve the component wavelengths and their phases, the wavelengths being given in terms of the unit block length of 50 bases used for determining the wavelength distribution. Continuous periodogram power spectral analyses of the fractal fluctuations in the frequency distribution of bases A, C, G, T in Drosophila DNA base sequence follow closely the following model predictions given in Section 2.

The variance spectra for the entire data sets exhibit the universal inverse power-law form $1/f^a$ of the statistical normal distribution (Figures 2 and 3) where f is the frequency and a, the spectral slope decreases with increase in wavelength (or decrease in frequency since frequency is inversely proportional to wavelength) and approaches I for long wavelengths. Inverse power-law form for power spectra imply long-range spatial correlations in the frequency distributions

of the bases A, C, G, T in Drosophila DNA base sequence structure. Fractal fluctuations exhibit scale invariance, namely the eddy amplitudes being related to each other by a simple proportionality factor for the range of wavelengths for which a is a constant. The observed frequency distribution exhibits multifractal structure since the slope a of the spectrum is not a constant, but decreases with increasing wavelength. Microscopic-scale quantum systems such as the electron or photon exhibit non-local connections or long-range correlations and are visualised to result from the superimposition of a continuum of eddies. Therefore, by analogy, the observed fractal fluctuations of frequency distribution of bases A, C, G, T exhibit quantumlike chaos in the Drosophila DNA base sequence structure.

Incidentally physics at the atomic scale is determined by the rules of quantum mechanics, which tells us that particles propagate like waves, and so can be described by a quantum mechanical wave function (Rae, 1999). As an immediate consequence, a particle can be in two or more states at the same time - a so-called superposition of states. This curious behaviour has been hugely successful in describing physical systems at the microscopic level. For example, under the rules of quantum mechanics two atoms sharing an electron form a chemical bond, whereas in classical theory the electron remains confined to one atom and the bond cannot form (Blatter, 2000).

• *Berry's phase*, namely, phase spectra and variance spectra being the same is seen in about 50% of the data sets (Figure 9). However, for all the data sets, the phase

spectra follow the variance spectra for a majority of dominant wavebands (Figure 6), particularly for the shorter wavelengths up to 4 - 6 unit block length of 50 bases. Microscopic scale quantum systems exhibit $Berry's\ phase$.

- The period T_{50} up to which the cumulative percentage contribution to total variance is equal to 50% is larger than the model predicted (Equation 7) value equal to 3.6 unit block length of 50 bases for a majority of data sets (Figure 9). This may indicate that the primary length scale may be less than the unit block length of 50 bases used for evaluating the frequency distribution.
- The power spectra exhibit dominant wavebands with peak wavelengths close to model predicted values (Equation 2). The average class interval-wise distribution of dominant wavelengths (Figure 4) and dominant wavelengths which exhibit Berry's phase (Figure 6) for all data sets show a maximum for the shorter wavelengths up to 4 6 unit block length of 50 bases. The dominant significant wavelengths show a maximum for wavelengths larger than 4 6 unit block length of 50 bases. This result is consistent with observed value of T_{50} being greater than the model predicted value equal to 3.6 unit block length of 50 bases as shown the earlier item above
- The bandwidth of the dominant waveband is directly proportional to the square of the corresponding peak wavelength (Figure 7) in agreement with model prediction (Equation 9).

5. Conclusions

Power spectra of frequency distribution of bases A, C, G, T of Drosophila DNA base sequence follow the model predicted universal and unique inverse power-law form of the statistical normal distribution.

Inverse power-law form for power spectra generic to *fractal* fluctuations is a signature of *self-organized criticality* in dynamical systems in nature. The author had shown earlier (Selvam and Suvarna Fadnavis, 1998; Selvam, 2001a, b) that (a) *self-organized criticality* can be quantified in terms of the universal inverse power-law form of the statistical normal distribution and (b) *self-organized criticality* of selfsimilar *fractal* fluctuations implies long-range space-time correlations and is a signature of quantumlike chaos in macro-scale dynamical systems of all space-time scales.

Inverse power-law form for power spectra of fluctuations in spatial distribution of bases A, C, G, T imply long-range spatial correlations, or in other words, persistence or long-term (length scale) memory of short-term fluctuations. The fine-scale structure of longer length scale fluctuations carry the signature of shorter length scale fluctuations. The cumulative integration of shorter length scale fluctuations generates longer length scale fluctuations (eddy continuum) with two-way ordered energy feedback between the fluctuations of all length scales (Equation 1). The eddy continuum acts as a robust unified whole fuzzy logic network with global response to local perturbations. Increase in random noise or energy input into the short-length scale fluctuations creates intensification of fluctuations of all other length scales in the eddy continuum and may be noticed immediately in shorter length scale fluctuations. Noise is therefore a precursor to signal.

Real world examples of noise enhancing signal has been reported in electronic circuits (Brown, 1996). Man-made, urbanisation related, greenhouse gas induced global warming (enhancement of small-scale fluctuations) is now held responsible for devastating anomalous changes in regional and global weather and climate in recent years (Selvam and Fadnavis, 1998). Noise and fluctuations are at the seat of all physical phenomena. It is well known that, in linear systems, noise plays a destructive role. However, an emerging paradigm for nonlinear systems is that noise can play a constructive role—in some cases information transfer can be optimized at nonzero noise levels. Another use of noise is that its measured characteristics can tell us useful information about the system itself. Problems associated with fluctuations have been studied since 1826 (Abbott, 2001).

The apparently irregular fractal fluctuations of the frequency distribution of bases A, C, G, T in Drosophila DNA base sequence self-organize spontaneously to generate the robust geometry of logarithmic spiral with the quasiperiodic *Penrose* tiling pattern for the internal structure. Conventional power spectral analyses resolves such a logarithmic spiral geometry as an eddy continuum with embedded dominant wavebands, the peak periodicities being functions of the golden mean and the primary perturbation length scale equal to block length of 50 bases used in the present study. Power spectral analyses of the frequency distribution of bases A, C, G, T in Drosophila DNA base sequence also exhibit the model predicted dominant wavebands. These dominant periodicities are intrinsic to the selfsimilar *fractal* fluctuations (space-time) of dynamical systems in nature. Quantum systems are also characterised by continuous irregular space-time fluctuations analogous to fractal fluctuations of macro-scale dynamical systems (Hey and Walters, 1989).

The quasicrystalline structure of the quasiperiodic *Penrose* tiling pattern underlies the apparently irregular distribution of the bases A,

C, G, T in Drosophila DNA base sequence. Historically, Schrodinger (1967) introduced a concept that the most essential part of a living cell - the chromosome fiber - may suitably called an aperiodic crystal (Gribbin, 1985). A periodic crystal, like one of common salt, can carry only a very limited amount of information. But an aperiodic crystal in which there is structure obeying certain fundamental laws, but no dull repetition can carry enormous amount of information (Gribbin, 1985). The space filling geometric figure of the Penrose tiling pattern has intrinsic local five-fold symmetry (Devlin, 1997) and also ten-fold symmetry. One of the three basic components of DNA, the deoxyribose is a five-carbon sugar and may represent the local five-fold symmetry of the quasicrystalline structure of the quasiperidic *Penrose* tiling pattern of the DNA molecule as a whole. The DNA molecule also shows tenfold symmetry in the arrangement of 10 bases per turn of the double helix (Watson and Crick, 1953). The study of plant phyllotaxis in botany shows that the quasicrystalline structure of the quasiperiodic *Penrose* tiling pattern provides maximum packing efficiency for seeds, florets, leaves, etc (Jean, 1994; Stewart, 1995; Mary Selvam, 1998). Quasicrystalline structure of the quasiperiodic Penrose tiling pattern may be the geometrical structure underlying the packing of 10^3 to 10^5 micrometer of DNA in a eukaryotic (higher organism) chromosome into a metaphase structure a few microns long.

The important result of the present study is that the observed fractal frequency distributions of the bases A, C, G, T of Drosophila DNA base sequence exhibit long-range spatial correlations or self-organized criticality generic to dynamical systems in nature. Therefore, artificial modification of base sequence structure at any location may have significant noticeable effect on the function of the DNA molecule as a whole. Further, the presence of introns may not

be redundant, but may serve to organise the effective functioning of the *exons* in the DNA molecule as a complete unit.

In summary, the precise geometrical pattern of the quasiperiodic Penrose tiling pattern underlies the apparently chaotic fractal frequency distribution of base sequence in Drosophila DNA. The spatial geometry of the DNA is therefore organized into a hierarchy of helical structures (vortices) such as those seen in turbulent fluid flows. Such a concept may explain the observed loops of DNA in metaphase chromosome (Grosveld and Fraser, 1997) and also the characteristic and reproducible banding pattern of polytene chromosome (Corces and Gerasimova, 1997). It is believed that the loop organization of chromatin is important not only for compaction and spatial organization of the chromatin, but also for the regulation of gene expression. Each loop domain may represent an independent unit of chromatin structure and gene activity (Luderus and van Driel, 1997). Audit et al. (2002) discuss analyses of results (wavelet transform) with regard to possible interpretations of the observed long-range correlations in terms of mechanisms that might govern the positioning and the dynamics of the nucleosome along the DNA chain through cooperative process. Shiba et al. (2002) assessed the significance of periodicities of DNA in the origin of genes by constructing such periodic DNAs. Herzel et al. (1999) show that correlations within proteins affect mainly the oscillations at distances below 35 bp. The long-ranging correlations up to 100 bp reflect primarily DNA folding. Since the topological state of genomic DNA is of importance for its replication, recombination and transcription, there is an immediate interest to obtain information about the supercoiled state from sequence periodicities (Herzel et al., 1998; 1999). Fourier transform analysis applied to a DNA sequence offers a great new avenue for extracting information on the evolution of a DNA sequence (Nagai et al., 2001). Ordered patterns organized in

hierarchical periodicities were identified in DNA subtelomeric sequences from two lower eukaryotes, P.falciparum and S.cerevisiae (Pizzi *et al.*, 1990). Identification of dominant periodicities in DNA sequence will help understand the important role of coherent structures in genome sequence organisation (Chechetkin and Turygin, 1995; J. Widom, 1996). Li (2002) has discussed meaningful applications of spectral analyses in DNA sequence analysis.

In the present study the author made use of single bases such as A, C, G or T rather than dimers AA, AG, AC, AT, GA, GG, etc. or trimers AAA, AAT, AAC, AAG, AGA, AGT, etc. Hence the results of the study may have some limitations in their interpretation that can be made in terms of biology. For example, biologists would like to know whether A+T-rich sequences appear nonrandomly every 5000 bp (base pair)? Or if AA/TT dimers appear nonrandomly every 200 bp (as nucleosomal linkers)? Or if other sequences appear once every 50 kb (as loop-attachment sites)? However the fractal results could still be of importance to biologists. For example, the average classinterval wise distribution of dominant periodicities show a peak in the wavelength interval 4-6 in units of 50bp, i.e. 200 to 300bp for all the four bases (see Figure 4 and Section 3.4.2). This predominant wavelength interval 200 to 300 bp may correspond to the first stage of DNA coiling (condensation) to form the basic nucleosome unit of the chromatin fibre. Further, the wavelength T_{50} up to which the cumulative percentage contribution to total variance is equal to 50 is shown in Figure 9 for all the 50 data sets used in the study. The value of T_{50} ranges from 5 to 15 in units of 50bp, i.e. from 250 to 750bp. However the value of T_{50} is close to 250 for a majority of data sets (Figure 9) indicating again the predominance of the first stage of DNA coiling to form nucleosomes. In view of the above the author is studying longer sequences to examine the ramifications of the results in biology.

Acknowledgements

The author is indebted to the anonymous referees for their valuable comments on the original manuscript, which were responsible for significant improvement in the interpretation of the results. The author is grateful to Dr. A. S. R. Murty for his keen interest and encouragement during the course of this study.

References

- Abbott, D., 2001: Overview: Unsolved problems of noise and fluctuations. *Chaos* **11(3)**, 526-538.
- Alcamo, E., 2001: *DNA Technology* 2nd Edition. Academic Press, New York, pp.339.
- Allegrini, P., Barbi, M., Grigolini, P., and West, B. J., 1996: Dynamical model for DNA sequences. *Physical Review E* **52(5)**, 5281-5296. http://linkage.rockefeller.edu/wli/dna_corr
- Anandan, J., 1992: The geometric phase. Nature 360, 307-313.
- Arber, A., 1950: *The Natural Philosophy of Plant Form*. Cambridge University Press, London.
- Arneodo, A., Bacry, E., Graves, P. V. and Muzy, J. F., 1995: Characterizing long-range correlations in DNA sequences from wavelet analysis. *Physical Review Letters* **74(16)**, 3293-3296. http://linkage.rockefeller.edu/wli/dna_corr/arneodo95.pdf
- Arneodo, A., Muzy, J.-F., and Sornette, D., 1998: 'Direct' causal cascade in the stock market. *European Physical J. B* **2**, 277-282.
- Audit, B., Thermes, C., Vaillant, C., d'Aubenton-Carafa, Y., Muzy, J. F. and Arneodo, A., 2001: Long-range correlations in genomic DNA: A signature of the nucleosomal structure. *Physical Review Letters* **86(11)**, 2471-2474. http://linkage.rockefeller.edu/wli/dna_corr/audit01.pdf
- Audit, B., Vaillant, C., Arneodo, A., d'Aubenton-Carafa, Y., Thermes, C., 2002: Long-range correlations between DNA bending sites: Relation to the structure and dynamics of nucleosomes. *Journal of Molecular Biology* **316(4)**, 903-918.

- Bak, P., Tang, C., Wiesenfeld, K., 1987: Self-organized criticality: an explanation of 1/f noise. *Phys. Rev. Lett.* **59**, 381-384.
- Bak, P.C., Tang, C., Wiesenfeld, K., 1988: Self-organized criticality. Phys. Rev. A. 38, 364 374.
- Bak, P., Chen, K., 1989: The physics of fractals. *Physica D* 38, 5-12.
- Bak, P., Chen, K., 1991: Self-organized criticality. Sci. Am. Jan., 26-33.
- Bak, P., Chen, K., Scheinkman, J. A., and Woodford, M., 1992: Self-organized criticality and fluctuations in economics. http://www.santafe.edu/sfi/publications/Abstracts/92-04-018abs.html
- Ball, P. 2000: Augmenting the alphabet. Nature Science Update 30 August.
- Bates, A. D. and Maxwell, A., 1993: *DNA Topology*. Oxford University Press, Oxford, pp.111.
- Berry, M. V., 1988: The geometric phase. Sci. Amer. Dec., 26-32.
- Blatter, G., 2000: Schrodinger's cat is now fat. Nature 406, 25-26.
- Brown, J., 1996: Where two worlds meet. New Scientist 18 May, 26-30.
- Buchanan, M., 1997: One law to rule them all. New Scientist 8 Nov., 30-35.
- Buldyrev, S. V., Goldberger, A. L., Havlin, S., Mantegna, R. N., Matsa, M. E., Peng, C. K., Simons, M. and Stanley, H. E., 1995: Long-range correlation properties of coding and non-coding DNA sequences GenBank analysis. *Physical Review E* **51**(**5**), 5084-5091. http://linkage.rockefeller.edu/wli/dna corr/buldyrev95.pdf
- Burroughs, W. J., 1992: *Weather Cycles: Real or Imaginary?* Cambridge University Press, Cambridge.
- Canavero, F. G., Einaudi, F., 1987: Time and space variability of atmospheric processes. *J. Atmos. Sci.* **44(12)**, 1589-1604.
- Capra, F., 1996: The web of life. Harper Collins, London, pp.311.
- Chatzidimitriou-Dreismann, C. A. and Larhammar, D., 1993: Scientific Correspondence, *Nature* **361**, 212-213. http://linkage.rockefeller.edu/wli/dna_corr
- Chechetkin, V. R. and Yu. Turygin, A., 1995: Search of hidden periodicities in DNA sequences. *Journal of Theoretical Biology* **175**, 477-494. http://linkage.rockefeller.edu/wli/dna_corr
- Chen, P., 1996a: Trends, shocks, persistent cycles in evolving economy business cycle measurement in time-frequency representation, The Chapter 13 in

- Nonlinear Dynamics and Economics, (eds.) W.A. Barnett, A. P. Kirman, and M. Salmon, Cambridge University Press, Cambridge, UK.
- Chen, P., 1996b: A random walk or color chaos on the stock market? time-frequency analysis of S&P Indexes. *Studies in Nonlinear Dynamics and Econometrics* **1(2)**, 87-103. http://mitpress.mit.edu/e-journals/SNDE/001/articles/v1n2002.pdf
- Claire, J., 1964: The stuff of life. Phoenix House, London, pp.67.
- Clark, A. G., 2001: The search for meaning in noncoding DNA. *Genome Research* 11, 1319-1320. http://linkage.rockefeller.edu/wli/dna_corr
- Corces, V. G. and Gerasimova, T. I., 1997: Chromatin domains and boundary elements. In *Nuclear Organization, Chromatin Structure, and Gene Expression*. pp. 83-94. (eds.) Roel Van Driel and Arie P Otte, Oxford University Press.
- Deering, W., West, B. J., 1992: Fractal physiology. *IEEE Engineering in Medicine and Biology*, **June**, 40-46.
- Devlin, K., 1997: *Mathematics: The Science of Patterns*. Scientific American Library, NY, p.101.
- Eatwell, J., Milgate, M., and Newman, P., 1991: *The New Palgrave: A Dictionary of Economics 3*, MacMillan Press, London.
- Farmer, J. D., 1999: Physicists attempt to scale the ivory towers of finance. *Computing in Science & Engineering* **November/December**, 26-39. http://www.santafe.edu/sfi/publications/Abstracts/99-10-073abs.html
- Feigenbaum, J. A., and Freund, P. G. O., 1997a: Discrete scaling in stock markets before crashes. http://xxx.lanl.gov/pdf/cond-mat/9509033 6 Sep 1995.
- Feigenbaum, J. A., and Freund, P. G. O., 1997b: Discrete scale invariance and the" second Black Monday". http://xxx.lanl.gov/pdf/cond-mat/9710324 29 Oct 1997.
- Feigenbaum, J. A., 2001a: A statistical analysis of log-periodic precursors to financial crashes. http://xxx.lanl.gov/pdf/cond-mat/0101031 28 February 2001.
- Feigenbaum, J. A., 2001b: More on a statistical analysis of log-periodic precursors to financial crashes. http://xxx.lanl.gov/pdf/cond-mat/0107445 20 July 2001.
- Freeman, G.R., 1987: Introduction. In: Freeman, G.R. (ed.), *Kinetics of Nonhomogenous Processes*. John Wiley and Sons, Inc., NY, pp. 1-18.

- Freeman, G.R., 1990: KNP89: Kinetics of non homogenous processes (KNP) and nonlinear dynamics. *Can. J. Phys.* **68**, 655-659.
- Ghashghaie, S., Breymann, P. J., Talkner, P., Dodge, Y., 1996: Turbulent cascades in foreign exchange markets. *Nature* **381**, 767-770.
- Ghil, M., 1994: Cryothermodynamics: the chaotic dynamics of paleoclimate. *Physica D* 77,130-159.
- Gleick, J., 1987: Chaos: Making a New Science. Viking, New York.
- Goldberger, A. L., Rigney, D. R., West, B. J., 1990: Chaos and fractals in human physiology. *Sci. Am.* **262(2)**, 42-49.
- Gopikrishnan, P., Plerou, V., Amaral, L. A. N., Meyer, M., Stanley, H. E., 1999: Scaling of the distribution of fluctuations of financial market indices. http://xxx.lanl.gov/cond-mat/9905305.
- Gribbin, J., 1985: *In search of the double helix*. Wildwood House Ltd., England, pp.362.
- Grosveld, F. and Fraser, P., 1997: Locus control of regions. In *Nuclear Organization, Chromatin Structure, and Gene Expression*. pp. 129-144. (eds.) Roel Van Driel and Arie P Otte, Oxford University Press.
- Guharay, S., Hunt, B. R., Yorke, J. A., White, O. R., 2000: Correlations in DNA sequences across the three domains of life. *Physica D* **146**, 388-396. http://linkage.rockefeller.edu/wli/dna_corr/guharay00.pdf
- Gutenberg, B., and Richter, R. F., 1944: Frequency of earthquakes in California. *Bull. Seis. Soc. Amer.* **34**, 185.
- Hao Bailin, Lee, H. and Zhang, S., 2000: Fractals related to long DNA sequences and complete genomes. *Chaos, Solitons and Fractals* **11(6)**, 825-836. http://linkage.rockefeller.edu/wli/dna_corr/haolee00.pdf
- Havlin S., Buldyrev S. V., Goldberger, A. L., Mantegna, R. N., Peng, C. K., Simons, M., Stanley, H. E., 1995: Statistical and linguistic features of DNA sequences. *Fractals* Jun 3, 269-84.
- Herzel, H., Weiss, O., and Trifonov, E. N., 1998: Sequence periodicity in complete genomes of Archaea suggests positive supercoiling. *Journal of Biomolecular Structure & Dynamics* **16(2)**, 341-345. http://linkage.rockefeller.edu/wli/dna_corr
- Herzel, H., Weiss, O., and Trifonov, E. N., 1999: 10-11 bp periodicities in complete genomes reflect protein structure and DNA folding. *Bioinformatics* **15(3)**, 187-193. http://linkage.rockefeller.edu/wli/dna_corr

- Hey, T. and Walters, P., 1989: *The Quantum Universe*. Cambridge University Press, Cambridge, pp.180.
- Holste, D., Grosse, I. and Herzel, H., 2001: Statistical analysis of the DNA sequence of human chromosome 22. *Physical Review E* **64**, 041917(1-9). http://linkage.rockefeller.edu/wli/dna_corr/holste01.pdf
- Hooge, C., Lovejoy, S., Schertzer, D., Pecknold, S., Malouin, J. F., Schmitt, F., 1994: Multifractal phase transitions: the origin of self-organized criticality in earthquakes. *Nonlinear Processes in Geophysics* **1**,191-197.
- Jenkinson, A. F., 1977: A Powerful Elementary Method of Spectral Analysis for use with Monthly, Seasonal or Annual Meteorological Time Series.

 Meteorological Office, London, Branch Memorandum No. 57, pp. 1-23.
- Jean R. V. 1994. *Phyllotaxis: A Systemic Study in Plant Morphogenesis*. Cambridge University Press, NY, USA.
- Kadanoff, L. P., 1996: Turbulent excursions. Nature 382, 116-117.
- Kane, R. P., 1996: Quasibiennial and quasitriennial oscillations in some atmospheric parameters. *PAGEOPH* **147(3)**, 567-583.
- Kolmogorov, A. N., 1941: The local structure of turbulence in incompressible liquids for very high Reynolds numbers. *C. R. Russ. Acad. Sci.* **30**, 301-305.
- Kolmogorov, A. N., 1962: A refinement of previous hypotheses concerning the local structure of turbulence in a viscous inhomogeneous fluid at high Reynolds number. *J. Fluid Mech.* **13**, 82-85.
- Levine, D., Steinhardt, J., 1984: Quasicrystals: A new class of ordered structures. *Phys.Rev.Letts.* **53(26)**, 2477-2480.
- Leone, F., 1992: *Genetics: the mystery and the promise*. TAB Books, McGraw Hill, Inc., pp.229.
- Li, W., 1992: Generating nontrivial long-range correlations and 1/f spectra by replication and mutation. *International Journal of Bifurcation and Chaos* **2(1)**, 137-154. http://linkage.rockefeller.edu/wli/dna_corr/l-ijbc92-l.html
- Li, W., and Kaneko, K., 1992: Long-range correlation and partial 1/f^a spectrum in a noncoding DNA sequence. *Europhysics Letters* **17(7)**, 655-660. http://linkage.rockefeller.edu/wli/dna_corr/l-epl92-lk.html
- Li, W., Marr, T. G., Kaneko, K., 1994: Understanding long-range correlations in DNA sequences. *Physica D* **75(1-3)**, 392-416; erratum: **82**, 217 (1995). http://arxiv.org/chao-dyn/9403002

- Li, W., 2002: Are spectral analyses useful for DNA sequence analysis? Proc. *DNA* in Chromatin, At the Frontiers of Biology, Biophysics, and Genomics, March 23-29. Arcachon, France. http://linkage.rockefeller.edu/wli
- Luderus, M. E. E. and van Driel, R., 1997: Nuclear matrix-associated regions. In *Nuclear Organization, Chromatin Structure, and Gene Expression*. pp. 99-115. (eds.) Roel Van Driel and Arie P Otte, Oxford University Press.
- Maddox, J., 1988a: Licence to slang Copenhagen? *Nature* 332, 581.
- $Maddox,\,J.,\,1988b;\,Turning\,phases\,into\,frequencies.\,\textit{Nature}\,\textbf{334},\,99.$
- Maddox, J., 1993: Can quantum theory be understood? *Nature* **361**, 493.
- Mandelbrot, B. B., 1975: On the geometry of homogenous turbulence with stress on the fractal dimension of the iso-surfaces of scalars. J. Fluid Mech. **72**, 401-416.
- Mandelbrot, B. B., 1977: Fractals: Form, Chance and Dimension. Freeman, San Francisco.
- Mantegna, R. N., Stanley, H. E., 1995: Scaling behaviour in the dynamics of an economic index. *Nature* **376**, 46-49.
- Mary Selvam, A., 1990: Deterministic chaos, fractals and quantumlike mechanics in atmospheric flows. *Canadian J. Physics* **68**, 831-841. http://xxx.lanl.gov/html/physics/0010046
- Mary Selvam, A., Pethkar, J. S., and Kulkarni, M. K., 1992: Signatures of a universal spectrum for atmospheric interannual variability in rainfall time series over the Indian Region. *Int'l J. Climatol*. **12**, 137-152.
- Mary Selvam, A., 1998: Quasicrystalline pattern formation in fluid substrates and phyllotaxis. In *Symmetry in Plants*, D. Barabe and R. V. Jean (Editors), World Scientific Series in Mathematical Biology and Medicine, Volume 4., Singapore, pp.795-809. http://xxx.lanl.gov/abs/chao-dyn/9806001
- Mohanty, A. K. and Narayana Rao, A. V. S. S., 2000: Factorial moments analyses show a characteristic length scale in DNA sequences. *Physical Review Letters* **84(8)**, 1832-1835. http://linkage.rockefeller.edu/wli/dna_corr/mohanty00.pdf
- Monin, A. S. Yaglom, A. M., 1975: *Statistical Hydrodynamics*. Vols. 1 and 2. MIT Press, Cambridge, Ma.
- Muller, A., Beugholt, C., 1996: The medium is the message. *Nature* **383**, 296-297.
- Nagai, N., Kuwata, K., Hayashi, T., Kuwata, H., and Era, S., 2001: Evolution of the periodicity and the self-similarity in DNA sequence: A Fourier transform

- analysis. *Japanese Journal of Physiology* **51(2)**:159-168. http://linkage.rockefeller.edu/wli/dna corr
- Nelson, D. R., 1986: Quasicrystals. Sci. Amer. 255, 42-51.
- Newman, M., 2000: The power of design. *Nature* **405**, 412-413.
- Omori, F., 1895: On the aftershocks of earthquakes. J. Coll. Sci. 7, 111.
- Peng, C.-K., Buldyrev, S. V., Goldberger, A. L., Havlin, S., Sciortino, F., Simons, M., and Stanley, H. E., 1992: Long-range correlations in nucleotide sequences. *Nature* **356**,168–170. http://linkage.rockefeller.edu/wli/dna_corr/l-nature92-p.html
- Pizzi, E., Liuni, S. and Frontali, C., 1990: Detection of latent sequence periodicities. *Nucleic Acids Research* **18(13)**, 3745-3752. http://linkage.rockefeller.edu/wli/dna_corr
- Plerou, V., Gopikrishnan, P., Amaral, L. A. L., Meyer, M., Stanley, H. E., 1999: Scaling of the distribution of price fluctuations of individual companies. http://xxx.lanl.gov/cond-mat/9907161.
- Prabhu, V. V. and Claverie, J. M., 1992: Correlations in intronless DNA. Scientific Correspondence. *Nature* **359**, 782. http://linkage.rockefeller.edu/wli/dna_corr
- Rae, A., 1988: *Quantum-physics: illusion or reality?* Cambridge University Press, New York, pp.129.
- Rae, A. I. M., 1999: Waves, particles and fullerenes. *Nature* 401, 651-653.
- Richardson, L. F., 1960: The problem of contiguity: an appendix to statistics of deadly quarrels. In: Von Bertalanffy, L., Rapoport, A., (eds.) *General Systems Year book of the society for general systems research*, **V**, pp 139-187, Ann Arbor, MI.
- Richardson, L. F., 1965: Weather Prediction by Numerical Process. Dover, Mineola, N.Y.
- Ruhla, C. 1992: *The Physics of Chance*. Oxford University Press, Oxford, pp.217.
- Sambamurty, A. V. S. S., 1999: *Genetics*. Narosa Publishing House, New Delhi, pp.757.
- Schrodinger, E., 1967: What is Life? Cambridge University Press, Cambridge.
- Schroeder, M., 1991: *Fractals , Chaos and Powerlaws*. W. H. Freeman and Co., N.Y.

- Selvam, A. M., and Joshi, R. R., 1995: Universal spectrum for interannual variability in COADS global air and sea surface temperatures. *Int'l. J. Climatol.* **15**, 613–623.
- Selvam, A. M., Pethkar, J. S., Kulkarni, M. K., and Vijayakumar, K., 1996: Signatures of a universal spectrum for atmospheric interannual variability in COADS surface pressure time series. *Int'l. J. Climatol.* **16**, 393-404.
- Selvam, A. M., and Fadnavis, S., 1998: Signatures of a universal spectrum for atmospheric interannual variability in some disparate climatic regimes. *Meteorology and Atmospheric Physics* **66**, 87-112. http://xxx.lanl.gov/abs/chao-dyn/9805028
- Selvam, A. M., and Suvarna Fadnavis, 1998: Cantorian fractal patterns, quantumlike chaos and prime numbers in atmospheric flows. *Chaos, Solitons and Fractals* (Submitted). http://xxx.lanl.gov/abs/chao-dyn/9810011
- Selvam, A. M., 2001a: Quantumlike chaos in prime number distribution and in turbulent fluid flows. http://xxx.lanl.gov/html/physics/0005067. Published with modification in the Canadian electronic journal *APEIRON* 8(3), 29-64. http://redshift.vif.com/JournalFiles/V08NO3PDF/V08N3SEL.PDF
- Selvam, A. M., 2001b: Signatures of quantumlike chaos in spacing intervals of non-trivial Riemann zeta zeros and in turbulent fluid flows.

 http://xxx.lanl.gov/html/physics/0102028. Published with modification in the Canadian electronic journal APEIRON 8(4), 10-40.

 http://redshift.vif.com/JournalFiles/V08NO4PDF/V08N4SEL.PDF
- Shiba, K., Takahashi, Y., and Noda, T., 2002: On the role of periodism in the origin of proteins. *Journal of Molecular Biology* **320(4)**, 833-840.
- Simon, R., Kimble, H. J., Sudarshan, E. C. G., 1988: Evolving geometric phase and its dynamical interpretation as a frequency shift: an optical experiment. *Phys. Rev. Letts.* **61(1)**, 19-22.
- Skinner, J. E., 1994: Low dimensional chaos in biological systems. *Bio/technology* **12**, 596-600.
- Som, A., Chattopadhyay, Chakrabarti, J. and Bandyopadhyay, D., 2001: Codon distributions in DNA. *Physical Review E* **63**, 1-8. http://linkage.rockefeller.edu/wli/dna_corr/som01.pdf
- Sornette, D., Johansen, A., and Bouchaud, J-P., 1995: Stock market crashes, precursors and replicas. http://xxx.lanl.gov/pdf/cond-mat/9510036 6 Oct 1995.

- Stanley, H. E., 1995: Powerlaws and universality. Nature 378, 554.
- Stanley, M. H. R., Amaral, L. A. N., Buldyrev, S. V., Havlin, S., Leschhorn, H. Maass, P., Salinger, M. A., Stanley H.E., 1996: Can statistical physics contribute to the science of economics? *Fractals* **4(3)**, 415-425.
- Stanley, H. E., Amaral, L. A. N., Buldyrev, S. V., Goldberger, A. L., Havlin, S., Hyman, B. T., Leschhorn, H., Maass, P., Makse, H. A., Peng, C.-K., Salinger, M. A., Stanley, M. H. R., Vishwanathan, G. M., 1996: Scaling and universality in living systems. *Fractals* **4(3)**, 427-451.
- Stanley, H. E., Afanasyev, V., Amaral, L. A. N., Buldyrev, S. V., Goldberger, A. L., Havlin, S., Leschhorn, H., Maass, P., Mantegna, R. N., Peng, C.-K., Prince, P. A., Salinger, M. A., Stanley, M. H. R., and Viswanathanan, G. M., 1996:
 Anomalous fluctuations in the dynamics of complex systems: from DNA and physiology to econophysics. *Physica A: Statistical and Theoretical Physics* 224(1-2), 302-321.
- Stanley, H. E., 2000: Exotic statistical physics: Applications to biology, medicine, and economics. *Physica A* 285, 1-17.
- Stanley H. E., Amaral, L. A. N., Gopikrishnan, P., and Plerou, V., 2000: Scale invariance and universality of economic fluctuations. Physica 283 A, 31-41.
- Stewart, I., 1992: Where do nature's patterns come from? New Scientist 135, 14.
- Stewart, I., 1995: Daisy, daisy, give your answer do. Sci. Amer. 272, 76-79.
- Thompson, D. W., 1963: *On Growth and Form*. 2nd Ed., Cambridge University Press.
- Voss, R., 1992: Evolution of long-range fractal correlations and 1/f noise in DNA base sequences. *Physical Review Letters* **68(25)**, 3805-3808.
- Voss, R. F., 1994: Long-range fractal correlations in DNA introns and exons. *Fractals* **2(1)**, 1-6.
- Wallace, J. M., Hobbs, P.V., 1977: *Atmospheric Science: An Introductory Survey*. Academic Press, N. Y.
- Watson, J. D. and Crick, F. H. C., 1953: A structure for deoxyribose nucleic acid. *Nature* **April 25**, 737-38.
- Watson, J. D., 1997: *The double helix*. Weidenfeld and Nicolson, London, pp.175.
- West, B. J., 1990a: Fractal forms in physiology. *Int'l. J. Modern Physics B* **4(10)**, 1629-1669.

- West, B. J., 1990b: Physiology in fractal dimensions. *Annals of Biomedical Engineering* **18**, 135-149.
- Widom, J., 1996: Short-range order in Two eukaryotic genomes: Relation to chromosome structure. *Journal of Molecular Biology* **259**, 579-588. http://linkage.rockefeller.edu/wli/dna_corr
- Yu, Z-G., Anh, V. V. and Wang, B., 2000: Correlation property of length sequences based on global structure of the complete genome. *Physical Review E* **63**, 011903(1-8). http://linkage.rockefeller.edu/wli/dna_corr/yu00.pdf